

Exercise 5.2

Question 1

State the property that is used in each of the following statements:

- (i) If $a \parallel b$, then $\angle 1 = \angle 5$.
- (ii) If $\angle 4 = \angle 6$, then $a \parallel b$.
- (iii) If $\angle 4 + \angle 5 = 180^\circ$, then $a \parallel b$.



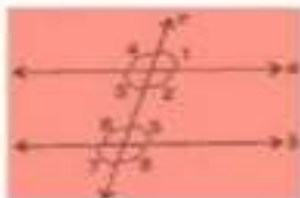
Answer 1:

- (i) If $a \parallel b$, then $\angle 1 = \angle 5$. [Corresponding angles]
If two parallel lines are cut by a transversal, each pair of corresponding angles are equal in measure.
- (ii) If $\angle 4 = \angle 6$, then $a \parallel b$. [Alternate interior angles]
When a transversal cuts two lines such that pairs of alternate interior angles are equal, the lines have to be parallel.
- (iii) If $\angle 4 + \angle 5 = 180^\circ$, then $a \parallel b$. [Co-interior Angles]
When a transversal cuts two lines, such that pairs of interior angles on the same side of transversal are supplementary, the lines have to be parallel.

Question 2

In the adjoining figure, identify:

- (i) The pairs of corresponding angles.
- (ii) The pairs of alternate interior angles.
- (iii) The pairs of interior angles on the same side of the transversal.
- (iv) The vertically opposite angles.

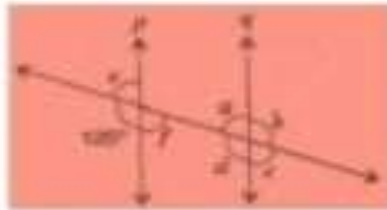


Answer 2:

- (i) The pairs of corresponding angles:
 $\angle 1, \angle 5; \angle 2, \angle 6; \angle 4, \angle 8$ and $\angle 3, \angle 7$
- (ii) The pairs of alternate interior angles are:
 $\angle 3, \angle 5$ and $\angle 2, \angle 6$
- (iii) The pair of interior angles on the same side of the transversal:
 $\angle 3, \angle 8$ and $\angle 2, \angle 5$
- (iv) The vertically opposite angles are:
 $\angle 1, \angle 3; \angle 2, \angle 4; \angle 6, \angle 8$ and $\angle 5, \angle 7$

Question 3

In the adjoining figure, $p \parallel q$. Find the unknown angles.

**Answer 3:**

Given, $p \parallel q$ and cut by a transversal line.

$$\begin{aligned} \therefore 125^\circ + x &= 180^\circ && \text{[Linear pair]} \\ \therefore x &= 180^\circ - 125^\circ = 55^\circ && \text{.....(i)} \\ \text{Now } x &= f = 55^\circ && \text{[Vertically opposite angles]} \\ \text{Also } x &= f = 55^\circ && \text{[Alternate interior angles]} \\ a + b &= 180^\circ && \text{[Linear pair]} \\ \therefore 55^\circ + b &= 180^\circ && \text{[From equation (i)]} \\ \therefore b &= 180^\circ - 55^\circ = 125^\circ \\ \text{Now } a &= c = 55^\circ \text{ and } b = d = 125^\circ && \text{[Vertically opposite angles]} \\ \text{Thus, } x &= 55^\circ, b = 125^\circ, a = 55^\circ, d = 125^\circ, c = 55^\circ \text{ and } f = 55^\circ. \end{aligned}$$

Question 4

Find the values of x in each of the following figures if $l \parallel m$.

**Answer 4:**

(i) Given, $l \parallel m$ and t is transversal line.

\therefore Interior vertically opposite angle between lines l and $l = 110^\circ$.

$\therefore 110^\circ + x = 180^\circ$ [Supplementary angles]

$\therefore x = 180^\circ - 110^\circ = 70^\circ$

(ii) Given, $l \parallel m$ and t is transversal line.

$x + 2x = 180^\circ$ [Interior opposite angles]

$\therefore 3x = 180^\circ$

$\therefore x = \frac{180^\circ}{3} = 60^\circ$

(iii) Given, $l \parallel m$ and $a \parallel b$.

$x = 100^\circ$ [Corresponding angles]